Similarity Search The q-Gram Distance

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Version November 9, 2016

Wintersemester 2016/2017

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Similarity Search

Filters for the Edit Distance Motivation

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Outline

Filters for the Edit Distance

- Motivation
- Lower Bound Filters
- Length Filter
- q-Grams: Count Filter
- q-Grams: Position Filtering
- Experiments
- The q-Gram Distance

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Filters for the Edit Distance Motivation Application Scenario

Scenario:

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- A company offers a number of services on the Web.
- You can subscribe for each service independently.
- Each service has its own database (no unique key across databases).
- Example: customer tables of two different services:

| А | | | | В | |
|---|------|------------------|------------|--------------------|--|
| | ID | name | ID | name | |
| | 1023 | Frodo Baggins | 948483 | John R. R. Tolkien | |
| | 21 | J. R. R. Tolkien | 153494 | C. S. Lewis | |
| | 239 | C.S. Lewis | 494392 | Fordo Baggins | |
| | 863 | Bilbo Baggins | 799294 | Biblo Baggins | |
| | | | | | |

Task: Created unified customer view!

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The Join Approach

• Solution: Join customer tables on name attribute (Q1):

```
SELECT * FROM A,B
WHERE A.name = B.name
```

- Exact Join: Does not work!
- Similarity Join: Allow k errors...
 - (1) Register UDF (User Defined Function) for the edit distance:

returns the union cost edit distance between the strings x and y.

(2) Rewrite query Q1 as similarity join (Q2):

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Filters for the Edit Distance Motivation

Using a Filter for Search Space Reduction

- Search space: $A \times B$ ($\Rightarrow |A| \cdot |B|$ edit distance computations)
- Filtering (Pruning): Remove tuples that can not match, without actually computing the distance.

Filters for the Edit Distance Motivation

Effectiveness and Efficiency of the Approximate Join

• Effectiveness: Join result for k = 3:

| ID | name | ID | name |
|------|------------------|--------|--------------------|
| 1023 | Frodo Baggins | 494392 | Fordo Baggins |
| 21 | J. R. R. Tolkien | 948483 | John R. R. Tolkien |
| 239 | C.S. Lewis | 153494 | C. S. Lewis |
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 \Rightarrow very good (100% correct)

- Efficiency: How does the DB evaluate the query?
 - (1) compute $A \times B$
 - (2) evaluate UDF on each tuple $t \in A \times B$
- Experiment [GIJ+01]: Self-join on string table (average string length = 14):

• 1K tuples: ca. 30min • 14K tuples: > 3 days!

Prohibitive runtime!

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Filters for the Edit Distance Lower Bound Filters

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Filters for the Edit Distance Lower Bound Filters

Filter Properties

Error Types:

Correct Result

| | | positive | negative |
|--------|----------|----------------|----------------|
| Filter | positive | true positive | false positive |
| Test | negative | false negative | true negative |

- Example: "Are x and y within edit distance k?"
 - Correct result: compute edit distance and test $ed(x, y) \le k$
 - Filter test: give answer without computing edit distance
 - False negatives: x and y are pruned although ed(x, y) < k.
 - False positives: x and y are not pruned although $ed(x, y) \nleq k$.
- Good filters have
 - no false negatives (i.e., miss no correct results)
 - few false positive (i.e., avoid unnecessary distance computations)

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Filters for the Edit Distance Length Filter

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Filters for the Edit Distance Lower Bound Filters

Lower Bound Filters

• Lower bound (lb) for distance dist(x, y):

$$dist(x, y) \ge lb_{dist}(x, y)$$

• Query Q3 with Lower Bound Filter :

```
SELECT * FROM A,B
WHERE 1b(A.name, B.name) <= k AND
      ed(A.name, B.name) <= k
```

- lb(A.name, B.name) is a cheap function
- database will optimize guery: compute ed (A.name, B.name) only if lb(A.name.B.name) > k
- No false negatives!

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Filters for the Edit Distance Length Filter

Length Filtering

Theorem (Length Filtering [GIJ $^+$ 01])

If two strings x and y are within edit distance k, their lengths cannot differ by more than k:

$$\operatorname{ed}(x,y) \ge \operatorname{abs}(|x| - |y|)$$

- Proof: At least abs(|x| |y|) inserts are needed to bring x and y to the same length.
- Query Q4 with Length Filtering:

```
SELECT * FROM A,B
WHERE ABS(LENGTH(A.name)-LENGTH(B.name)) <= k AND
      ed(A.name, B.name) <= k
```

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Filters for the Edit Distance Length Filter

Example: Length Filtering

• Execute query without/with length filter (k = 3):

| Α | | | В | | |
|---|------|--------------------------------|---|--------|----------------------------------|
| | ID | ID name | | ID | name |
| | 1023 | Frodo Baggins ₁₃ | | 948483 | John R. R. Tolkien ₁₈ |
| | 21 | J. R. R. Tolkien ₁₆ | | 153494 | C. S. Lewis ₁₁ |
| | 239 | C.S. Lewis ₁₀ | | 494392 | Fordo Baggins ₁₃ |
| | 863 | Bilbo Baggins ₁₃ | | 799294 | Biblo Baggins ₁₃ |

- Without length filter: 16 edit distance computations
- With length filter (k = 3): 12 edit distance computations
 - ullet J. R. R. Tolkien \leftrightarrow C. S. Lewis is pruned
 - all pairs (..., John R. R. Tolkien) except (J. R. R. Tolkien, John R. R. Tolkien) are pruned

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Filters for the Edit Distance q-Grams: Count Filter

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What is a *q*-Gram?

- Intuition:
 - slide window of length q over string $x \in \Sigma^*$
 - characters covered by window form a q-gram
 - where window extends string: fill with dummy character # $\notin \Sigma$
- Example: x = Frodo, q = 3

- q-Gram Profile G_x : bag of all q-grams of x
- Profile size: $|G_x| = |x| + q 1$

Filters for the Edit Distance q-Grams: Count Filter

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Filters for the Edit Distance q-Grams: Count Filter Single Edit Operations and Changing q-Grams

- Intuition: Strings within small edit distance share many q-grams.
- How many q-grams (q = 3) change/remain?

| X | $ G_x $ | у | $ G_y $ | $ G_x \cap G_y $ |
|-------|---------|--------|---------|------------------|
| peter | 7 | meter | 7 | 4 |
| peter | 7 | peters | 8 | 5 |
| peter | 7 | peer | 6 | 4 |

 \bullet ed $(x,y) = 1 \Rightarrow |G_x \cap G_y| = \max(|G_x|, |G_y|) - q$

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Multiple Edit Operations and Changing q-Grams

- $\bullet \ \operatorname{ed}(x,y) = 1 \Rightarrow |G_x \cap G_y| = \max(|G_x|, |G_y|) q$
- What if ed(x, v) = k > 1?

| X | $ G_x $ | у | $ G_y $ | $ G_x \cap G_y $ |
|-------|---------|--------|---------|------------------|
| peter | 7 | meters | 8 | 2 |
| peter | 7 | petal | 7 | 3 |

• Multiple edit operations may affect the same q-gram:

peter
$$\rightarrow G_x = \{ \#p, \#pe, pet, ete, ter, er\#, r\#\# \}$$

petal $\rightarrow G_x = \{ \#p, \#pe, pet, eta, tal, al\#, l\#\# \}$

• Each edit operation affects at most q q-grams.

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Filters for the Edit Distance q-Grams: Count Filter

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Implementation of *q*-Grams

- Given: tables A and B with schema (id, name)
 - id is the key attribute
 - name is string-valued
- Compute auxiliary tables QA and QB with schema (id, qgram):
 - each tuple stores one q-gram
 - string x of attribute *name* is represented by its |x| + q 1 q-grams
 - QA.id is the key value (A.id) of a tuple with A.name = x
 - QA.qgram is one of the q-grams of x
- Example:

| name Frodo Baggins | | id | qgram |
|-----------------------------|------------|------------|--------------------------------|
| Frodo Baggins | | 1000 | |
| J. R. R. Tolkien | | 1023 | ##F #Fr |
| C.S. Lewis Bilbo Baggins | | 21 21 | ##J #J. |
| | C.S. Lewis | C.S. Lewis | C.S. Lewis Bilbo Baggins 21 |

Filters for the Edit Distance q-Grams: Count Filter

Count Filtering

Theorem (Count Filtering [GIJ⁺01])

Consider two strings x and y with the q-gram profiles G_x and G_y , respectively. If x and y are within edit distance k, then the cardinality of the q-gram profile intersection is at least

$$|G_x \cap G_y| \ge \max(|G_x|, |G_y|) - kq$$

- Proof (by induction):
 - true for k = 1: $|G_x \cap G_y| \ge \max(|G_x|, |G_y|) q$
 - $k \rightarrow k + 1$: each additional edit operation changes at most q *q*-grams. □

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Filters for the Edit Distance q-Grams: Count Filter

Count Filtering Query

• Query Q5 with Count Filtering:

SELECT A.id, B.id, A.name, B.name

FROM A, QA, B, QB

A.id = QA.id AND WHERE B.id = QB.id AND

QA.qgram = QB.qgram AND

ABS(LENGTH(A.name)-LENGTH(B.name)) <= k

GROUP BY A.id, B.id, A.name, B.name

COUNT(*) >= LENGTH(A.name)-1-(k-1)*q ANDHAVING

COUNT(*) >= LENGTH(B.name)-1-(k-1)*q AND

ed(A.name,B.name) <= k

Filters for the Edit Distance q-Grams: Count Filter

Problem with Count Filtering Query

- Previous query Q5 works fine for $kq < \max(|G_x|, |G_y|)$.
- However: If $kq > \max(|G_x|, |G_y|)$, no q-grams may match even if $ed(x, y) \le k$.
- Example (q = 3, k = 2): WHERE-clause prunes x and y, although ed(x, y) $\leq k$

- False negatives:
 - short strings with respect to edit distance (e.g., |x| = 3, k = 3)
 - even if within given edit distance, matches tend to be meaningless (e.g., abc and xyz are within edit distance k = 3)

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Filters for the Edit Distance q-Grams: Position Filtering

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Filters for the Edit Distance q-Grams: Count Filter

Fixing Count Filtering Query

- Fix query to avoid false negatives [GIJ+03]:
 - Join pairs (x, y) with $kq \ge \max(|G_x|, |G_y|)$ using only length filter.
 - Union results with results of previous query Q5.
- Query Q6 without false negatives (extends previous query Q5):

```
UNION
SELECT A.id, B.id, A.name, B.name
FROM A, B
WHERE LENGTH(A.name)+q-1 \leq k*q AND
       LENGTH(B.name)+q-1 \le k*q AND
       ABS(LENGTH(A.name) - LENGTH(B.name)) <= k AND
       ed(A.name.B.name) <= k
```

• Note: We omit this part in subsequent versions of the query since it remains unchanged.

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Filters for the Edit Distance q-Grams: Position Filtering

Positional q-Grams

- Enrich *q*-grams with position information:
 - extended string: prefix and suffix string x with q-1 characters #
 - slide window of length q over extended string x'
 - characters covered by window after shifting it i times form the q-gram at position i + 1

(7,0 # #)

• Example: x = Frodo

```
extended string:
                         ##Frodo##
positional q-grams:
                     (1, # # F)
                       (2, \# Fr)
                        (3.Fro)
                          (4,r o'd)
                            (5.0 do)
                             (6.d o \#)
```

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Filters for the Edit Distance q-Grams: Position Filtering

Computing Positional q-Grams in SQL

- Given: table N
 - N has a single attribute i
 - N is filled with numbers from 1 to max (max is the maximum string length plus q-1)
- Positional q-grams for table A in SQL (Q7):

```
CREATE TABLE QA AS
      SELECT A.id, N.i AS pos,
           SUBSTRING(CONCAT(
               SUBSTRING('#..#', 1, q - 1),
               LOWER(A.name),
               SUBSTRING('#..#', 1, q - 1)),
           N.i, q) AS ggram
       FROM A, N
      WHERE N.i <= LENGTH(A.name) + q - 1
```

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Filters for the Edit Distance q-Grams: Position Filtering

Position Filtering

Theorem (Position Filtering [GIJ+01])

If two strings x and y are within edit distance k, then a positional q-gram in one cannot correspond to a positional q-gram in the other that differs from it by more then k positions.

- Proof:
 - each increment (decrement) of a position requires an insert (delete);
 - a shift by k positions requires k inserts/deletes.

Filters for the Edit Distance q-Grams: Position Filtering

Corresponding q-Grams

- Corresponding *q*-gram:
 - Given: positional q-grams (i, g) of x
 - transform x to y applying edit operations
 - (i,g) "becomes" (i,g) in y
 - We define: (i,g) corresponds to (j,g)
- Example:
 - x' = #abaZabaabaaba##, y' = #abaabaabaabaaba##
 - edit distance is 1 (delete Z from x)
 - (7, aba) in x corresponds to (6, aba) in y
 - ... but not to (9, aba)

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Filters for the Edit Distance q-Grams: Position Filtering

Position Filtering

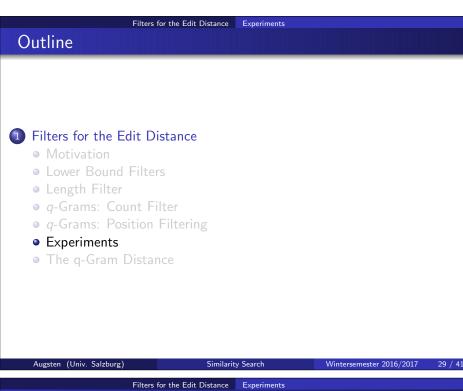
SELECT

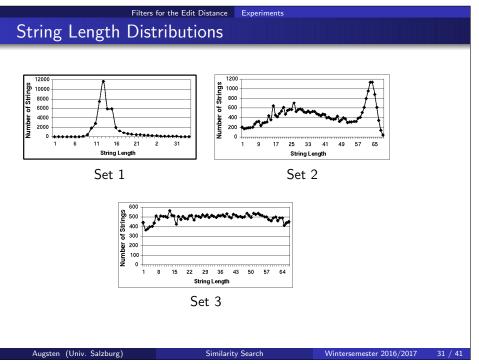
Query Q8 with Count and Position Filtering:

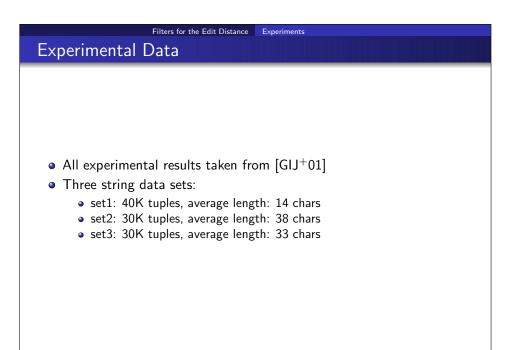
```
A.id, B.id, A.name, B.name
FROM
         A, QA, B, QB
WHERE
         A.id = QA.id AND
         B.id = QB.id AND
         QA.qgram = QB.qgram AND
         ABS(LENGTH(A.name)-LENGTH(B.name)) <= k AND
         ABS(QA.pos-QB.pos) <= k
GROUP BY A.id, B.id, A.name, B.name
```

HAVING COUNT(*) >= LENGTH(A.name)-1-(k-1)*q ANDCOUNT(*) >= LENGTH(B.name)-1-(k-1)*q ANDed(A.name,B.name) <= k

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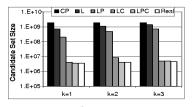
• Question: How many edit distances do we have to compute?

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• Show candidate set size for different filters (small is good).

Filters for the Edit Distance Experiments

- q = 2
- Caption:
 - CP: cross product
 - L: length filtering, P: position filtering, C: count filtering
 - Real: number of real matches



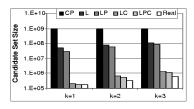
Set 1

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Filters for the Edit Distance Experiments

Candidate Set Size

- Question: How many edit distances do we have to compute?
- Show candidate set size for different filters (small is good).
- q = 2
- Caption:
 - CP: cross product
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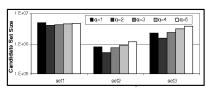
Set 2

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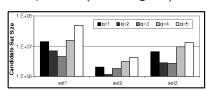
Filters for the Edit Distance Experiments

Various q-Gram Lengths

- Question: How does the choice of *q* influence the filter effectiveness?
- Show candidate set size for different q values (small is good).



Edit Distance Threshold k = 2

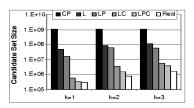


Edit Distance Threshold k = 3

Filters for the Edit Distance Experiments

Candidate Set Size

- Question: How many edit distances do we have to compute?
- Show candidate set size for different filters (small is good).
- q = 2
- Caption:
 - CP: cross product
 - L: length filtering, P: position filtering, C: count filtering
 - Real: number of real matches



Set 3

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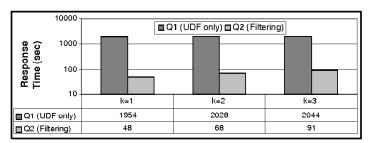
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Response Time

- Approximate self-join on small sample of 1000 tuples (set 1) (full dataset > 3 days without filters!)
- Measure response time (small is good).
- Caption:

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- k: edit distance threshold
- Q1: edit distance without filters
- Q2: edit distance with filters



Filters for the Edit Distance The q-Gram Distance

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Filters for the Edit Distance The g-Gram Distance

Pseudo Metric q-Gram Distance

• The q-gram distance is a pseudo metric:

For all $x, y, z \in \Sigma^*$

- $\operatorname{dist}_{a}(x, y) + \operatorname{dist}_{a}(y, z) \geq \operatorname{dist}_{a}(x, z)$ (triangle inequality)
- $\operatorname{dist}_{a}(x, y) = \operatorname{dist}_{a}(y, x)$ (symmetric)
- $\operatorname{dist}_{a}(x, y) = 0 \Leftarrow x = y$
- Note: Identity condition relaxed: $dist_{\sigma}(x, y) = 0 \Rightarrow x = y$ i.e., the q-gram distance between two different strings can be 0
- Example:

$$\begin{aligned} &\mathsf{dist}_q(\mathtt{axybxycxyd},\mathtt{axycxybxyd}) = 0 \\ &G_x = G_y = \{ \texttt{\##a}, \texttt{\#ax}, \mathtt{axy}, \mathtt{xyb}, \mathtt{ybx}, \mathtt{bxy}, \mathtt{xyc}, \mathtt{ycx}, \mathtt{cxy}, \mathtt{xyd}, \mathtt{yd\#}, \mathtt{d\#\#} \} \end{aligned}$$

Filters for the Edit Distance The q-Gram Distance

The q-Gram Distance

Definition (q-Gram Distance [Ukk92])

Let G_x and G_y be the q-gram profiles of the strings x and y, respectively. The q-gram distance between two strings is the number of q-grams in G_x and G_{v} that have no match in the other profile,

$$\mathsf{dist}_q(x,y) = |G_x \uplus G_y| - 2|G_x \cap G_y|.$$

• Example: q = 2, x = abab, y = abcab $G_{x} = \{\text{#a, ab, ba, ab, b#}\}$ $G_v = \{ \text{#a, ab, bc, ca, ab, b#} \}$

 $G_x \uplus G_y = \{ \text{\#a,ab,ba,ab,b\#,\#a,ab,bc,ca,ab,b\#} \}$ $G_x \cap G_v = \{\text{\#a,ab,ab,b\#}\}$

$$dist_q(x, y) = |G_x \uplus G_y| - 2|G_x \cap G_y| = 11 - 2 \cdot 4 = 3$$

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Filters for the Edit Distance The q-Gram Distance

Distance Normalization (1/3)

• What is a good threshold?

ed(International Business Machines Corporation, International Bussiness Machine Corporation) = 2ed(IBM, BMW) = 2ed(Int. Business Machines Corp., International Business Machines Corporation) = 17

- Problem: Absolute numbers not always meaningful...
- Solution: Compute error relative to string length!

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Filters for the Edit Distance The q-Gram Distance

Distance Normalization (2/3)

• Normalize distance such that $\delta(x, y) \in [0..1]$

• Edit Distance: 0 < ed(x, y) < max(|x|, |y|)

• Normalized Edit Distance: 0 < norm-ed(x, y) < 1

$$norm-ed(x,y) = \frac{ed(x,y)}{max(|x|,|y|)}$$

- q-Gram Distance: $0 \le \operatorname{dist}_q(x, y) \le |G_x \uplus G_v| |G_x \cap G_v|$
- Normalized *q*-Gram Distance: $0 < \text{norm-dist}_{q}(x, y) < 1$

$$\mathsf{norm\text{-}dist}_q(x,y) = \frac{\mathsf{dist}_q(x,y)}{|G_x \uplus G_y| - |G_x \cap G_y|} = 1 - \frac{|G_x \cap G_y|}{|G_x \uplus G_y| - |G_x \cap G_y|}$$

• Dividing by $|G_x \uplus G_y|$ also normalizes to [0..1], but the metric properties (triangle inequality) get lost [ABG10].

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Filters for the Edit Distance The g-Gram Distance

Edit Distance vs. q-Gram Distance

- Edit distance can not handle block-moves well:
 - x =Nikolaus Augsten y =Augsten Nikolaus norm-ed(x, y) = 1.0norm-dist_q $(x, y) = 0.39 \quad (q = 3)$
- *q*-Gram distance may be too strict:

```
x = +39-06-46-74-22 y = (39\ 06\ 467422)
norm-ed(x, y) = 0.4
norm-dist<sub>q</sub>(x, y) = 1.0 \quad (q = 3)
```

Filters for the Edit Distance The q-Gram Distance

Distance Normalization (3/3)

Normalized edit distance:

```
norm-ed(International Business Machines Corporation.
       International Bussiness Machine Corporation) = 0.047
norm-ed(IBM, BMW) = 0.66
norm-ed(Int. Business Machines Corp...
       International Business Machines Corporation) = 0.4
```

• Normalized q-gram distance (q = 3):

```
norm-dist<sub>a</sub>(International Business Machines Corporation,
          International Bussiness Machine Corporation) = 0.089
norm-dist_a(IBM, BMW) = 1.0
norm-dist<sub>a</sub>(Int. Business Machines Corp.,
          International Business Machines Corporation = 0.36
```

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- Luis Gravano, Panagiotis G. Ipeirotis, H. V. Jagadish, Nick Koudas, S. Muthukrishnan, and Divesh Srivastava. Approximate string joins in a database (almost) for free. In Proceedings of the International Conference on Very Large Databases (VLDB), pages 491-500, Roma, Italy, September 2001. Morgan Kaufmann Publishers Inc.
- Luis Gravano, Panagiotis G. Ipeirotis, H. V. Jagadish, Nick Koudas, S. Muthukrishnan, and Divesh Srivastava. Approximate string joins in a database (almost) for free — Erratum. Technical Report CUCS-011-03, Department of Computer Science, Columbia University, 2003.
- Esko Ukkonen.

Approximate string-matching with q-grams and maximal matches.

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