Similarity Search

Trees

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Outline

1. What is a Tree?
2. Encoding XML as Trees

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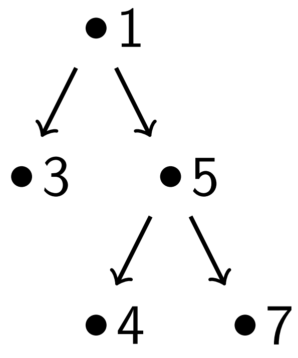
2. Encoding XML as Trees

What is a Tree?

- Graph: a pair (N, E) of nodes N and edges E between nodes of N
- Tree: a directed, acyclic graph T
  - that is connected and
  - no node has more than one incoming edge
- Edges: $E(\mathrm{T})$ are the edges of T
  - an edge $(\mathrm{p}, \mathrm{c}) \in E(\mathrm{T})$ is an ordered pair
  - with $\mathrm{p}, \mathrm{c} \in N(\mathrm{T})$
- "Special" Nodes: $N(\mathrm{T})$ are the nodes of T
  - parent/child: $(\mathrm{p}, \mathrm{c}) \in E(T) \Leftrightarrow$ p is the parent of c, c is the child of p
  - siblings: c_1 and c_2 are siblings if they have the same parent node
  - root node: node without parent (no incoming edge)
  - leaf node: node without children (no outgoing edge)
  - fanout: fanout f_v of node v is the number of children of v

Unlabeled Trees

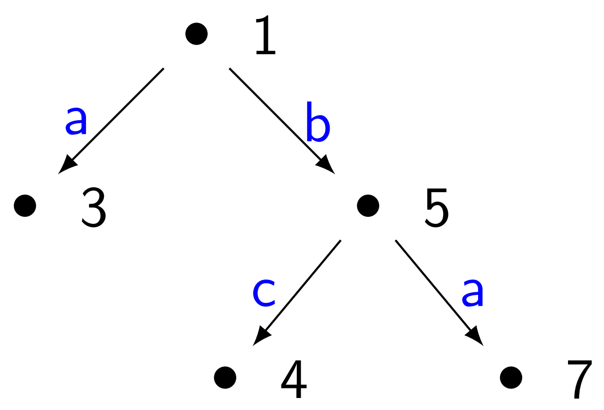
- Unlabeled Tree:
  - the focus is on the structure, not on distinguishing nodes
  - however, we need to distinguish nodes in order to define edges
    $\Rightarrow$ each node v has a unique identifier id(v) within the tree
- Example: $T = (\{1, 3, 5, 4, 7\}, \{(1, 3), (1, 5), (5, 4), (5, 7)\})$



Edge Labeled Trees

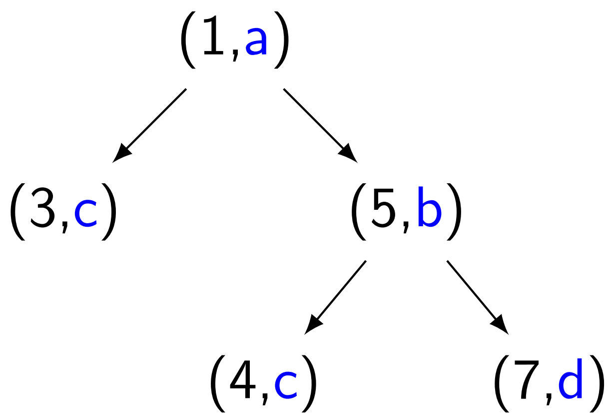
- Edge Labeled Tree:
  - an edge $e \in E(\mathrm{T})$ between nodes a and b is a triple $e = (\mathrm{id}(a), \mathrm{id}(b), \lambda(e))$
  - id(a) and id(b) are node IDs
  - $\lambda(e)$ is the edge label (not necessarily unique within the tree)
- Example:

$$\mathrm{T} = (\{1,3,5,4,7\}, \{(1,3,\mathtt{a}), (1,5,\mathtt{b}), (5,4,\mathtt{c}), (5,7,\mathtt{a})\})$$



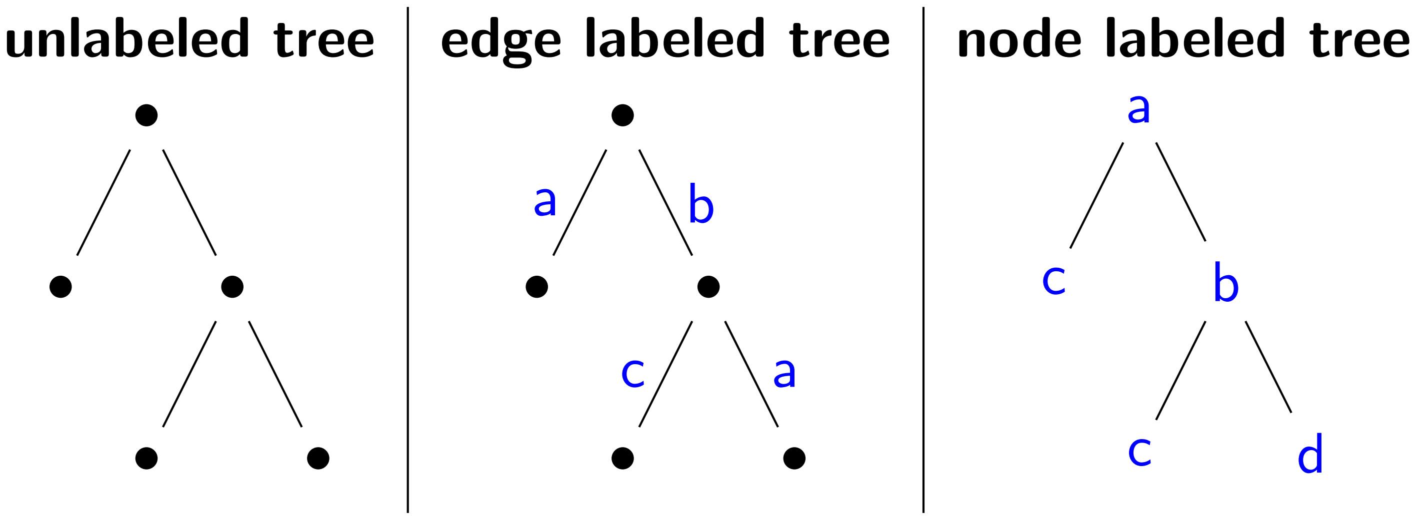
Node Labeled Trees

- Node Labeled Tree:
  - a node $v \in N(T)$ is a pair $(id(v), \lambda(v))$
  - id(v) is unique within the tree
  - label $\lambda(v)$ needs not to be unique
- Intuition:
  - The identifier is the key of the node.
  - The label is the data carried by the node.
- Example: $T = (\{(1, a), (3, c), (5, b), (4, c), (7, d)\},$
  $\{(1, 3), (1, 5), (5, 4), (5, 7)\})$



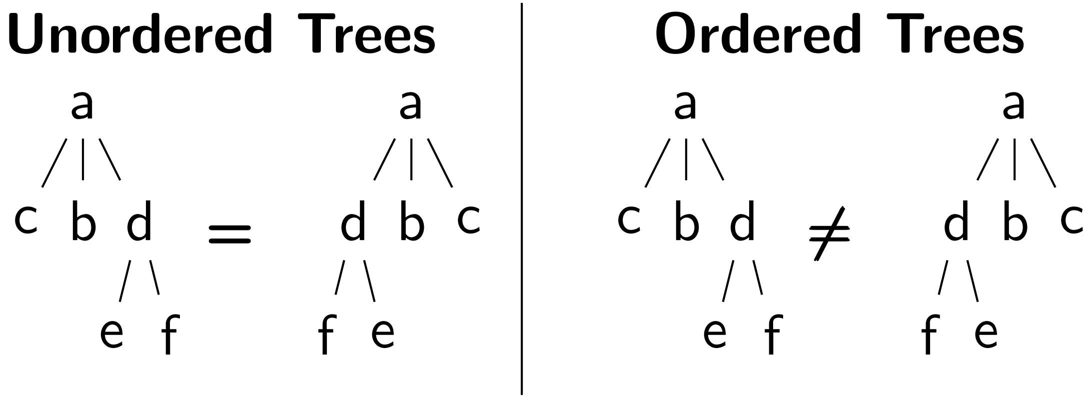
Notation and Graphical Representation

- Notation:
  - node identifiers: $\text{id}(v_i) = i$
  - tree identifiers: $T_1, T_2, \ldots$
- Graphical representation
  - we omit brackets for (identifier,label)-pairs
  - we (sometimes) omit node identifiers at all
  - we do not show the direction of edges (edges are always directed from root to leave)



Ordered Trees

- Ordered Trees: siblings are ordered
- contiguous siblings $s_1 < s_2$ have no sibling x such that $s_1 < x < s_2$
- c_i is the *i*-th child of p if
  - p is the parent of c_i, and
  - $i = |\{x \in N(T) : (p, x) \in E(T), x \leq c_i\}|$
- Example:

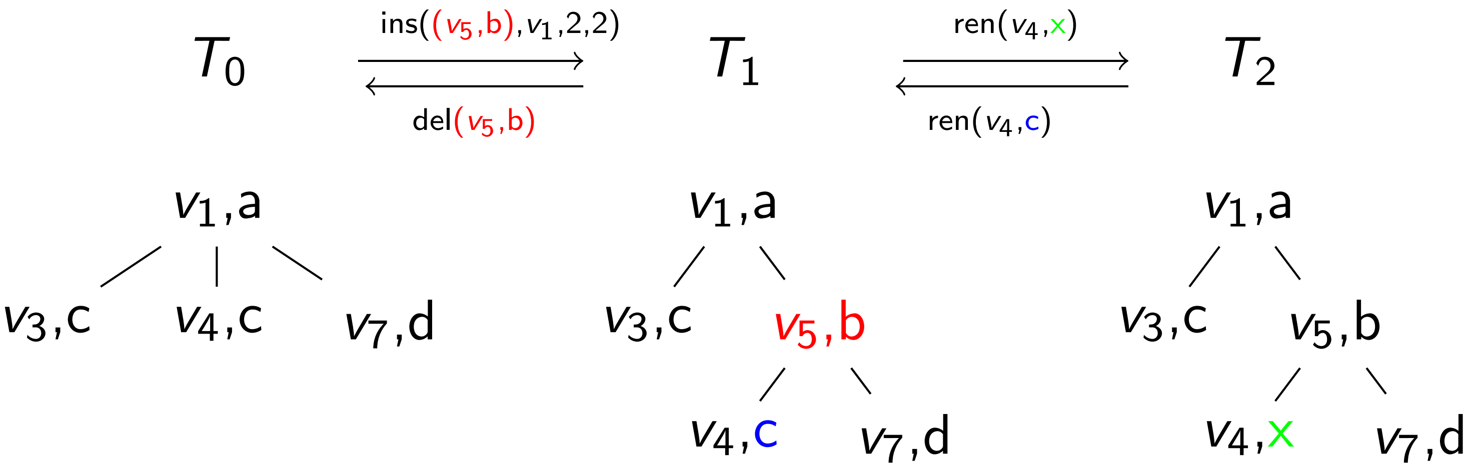


- Note: "ordered" does not necessarily mean "sorted alphabetically"

Edit Operations

- We assume ordered, labeled trees
- Rename node: $ren(\mathrm{v}, l')$
  - change label l of v to $l' \neq l$
- Delete node: $del(\mathrm{v})$ (v is not the root node)
  - remove v
  - connect v's children directly to v's parent node (preserving order)
- Insert node: $ins(\mathrm{v}, \mathrm{p}, k, m)$
  - detach m consecutive children of p, starting with the child at position k, i.e., the children $c_k, c_{k+1}, \ldots, c_{k+m-1}$
  - attach $c_k, c_{k+1}, \ldots, c_{k+m-1}$ as children of the new node v (preserving order)
  - insert new node v as k-th child of p
- Insert and delete are inverse edit operations (i.e., insert undoes delete and vice versa)

Example: Edit Operations



Outline

1 What is a Tree?

2 Encoding XML as Trees

Representing XML as a Tree

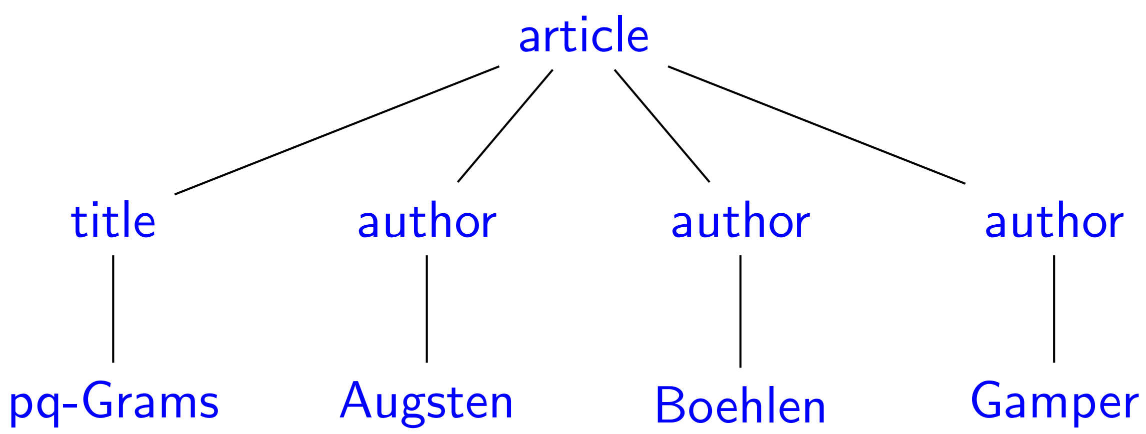
- Many possibilities – we will consider
  - single-label tree
  - double-label tree
- Pros/cons depend on application!

XML as a Single-Label Tree

- The XML document is encoded as a tree with:
    - XML element: node labeled with element tag name
    - XML attribute: node labeled with attribute name
    - Text contained in elements/attributes: node labeled with the text-value
- Element nodes contain:
    - nodes of their sub-elements
    - nodes of their attributes
    - nodes with their text values
- Attribute nodes contain:
    - single node with their text value
- Text nodes are always leaves
- Order:
    - sub-element and text nodes are ordered
    - attributes are not ordered (approach: store them before all sub-elements, sort according to attribute name)

Example: XML as a Single-Label Tree

```
<article title='pq-Grams'>
  <author>Augsten</author>
  <author>Boehlen</author>
  <author>Gamper</author>
</article>
```



XML as a Double-Label Tree

- Node labels are pairs
- The XML document is encoded as a tree with:
  - XML element: node labeled with (tag-name,text-value)
  - XML attribute: node labeled with (attribute-name,text-value)
- Element nodes contain:
  - nodes of their sub-elements and attributes
- Attribute nodes are always leaves
- Element nodes without attributes or sub-elements are leaves
- Order:
  - sub-element nodes are ordered
  - attributes are not ordered (approach: see previous slide)
- Limitation: Can represent
  - *either* elements with sub-elements and/or attributes
  - *or* elements with a text value

Example: XML as a Double-Label Tree

```
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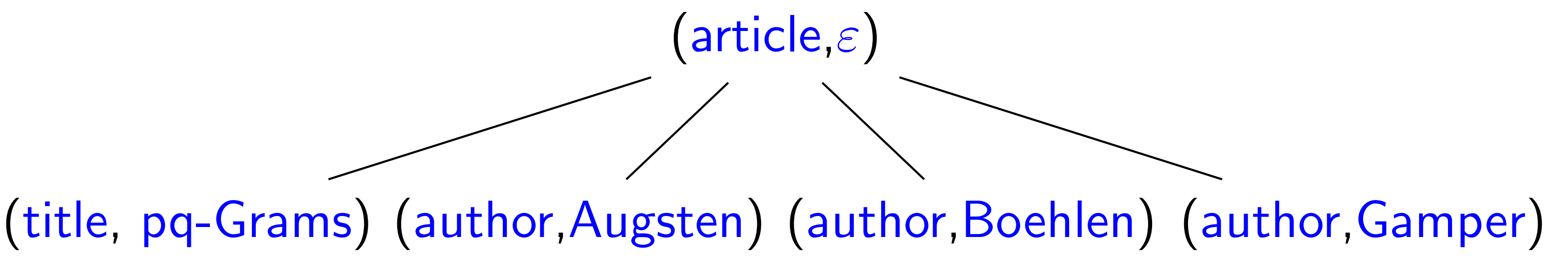
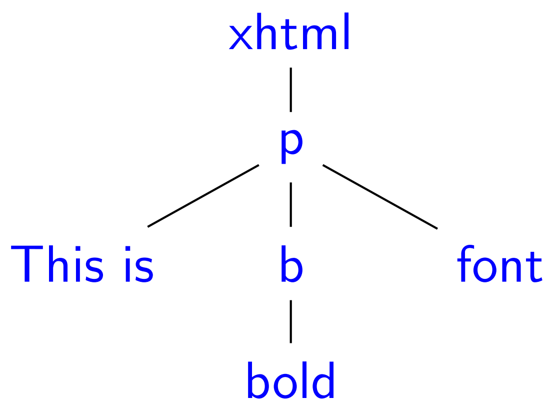


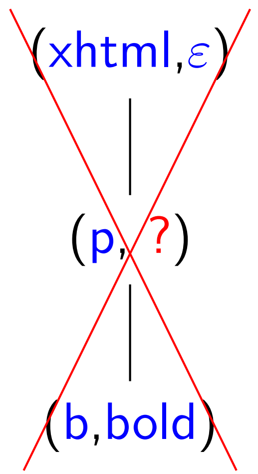
Example: Single- vs. Double-Label Tree

```
<xhtml>
  <p>This is <b>bold</b> font.</p>
<xhtml>
```

Single-Label Tree



Double-Label Tree



Parsing XML

We discuss two popular parsers for XML:

- DOM – Document Object Model
- SAX – Simple API for XML
- StAX – Streaming API for XML

DOM – Document Object Model

- W3C[1] standard for accessing and manipulating XML documents
- Tree-based: represents an XML document as a tree (single-label tree with additional node info, e.g. node type)
- Elements, attributes, and text values are nodes
- DOM parsers load XML into main memory
  - random access by traversing tree :-)
  - large XML documents do not fit into main memory :-(

[1] `http://www.w3schools.com/dom`

SAX / StAX

- SAX – Simple API for XML[2]
  - ‘de facto” standard for parsing XML
- Event-based: reports parsing events (e.g., start and end of elements)
  - no random access :-(
  - you see only one element/attribute at a time
  - you can parse (arbitrarily) large XML documents :-)
- StAX - Streaming API for XML[3]
  - similar to SAX, but pull-based (vs. SAX: push)
  - pull: the client receives the next event on request
- Java API available for DOM, SAX, and StAX.
- For importing XML into a database: use SAX or StAX!

[2] http://www.saxproject.org

[3] https://en.wikipedia.org/wiki/StAX