# Similarity Search in Large Databases Introduction to Similarity Search

Nikolaus Augsten

nikolaus.augsten@plus.ac.at Department of Computer Science University of Salzburg



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Similarity Search in Large Databases



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# Outline

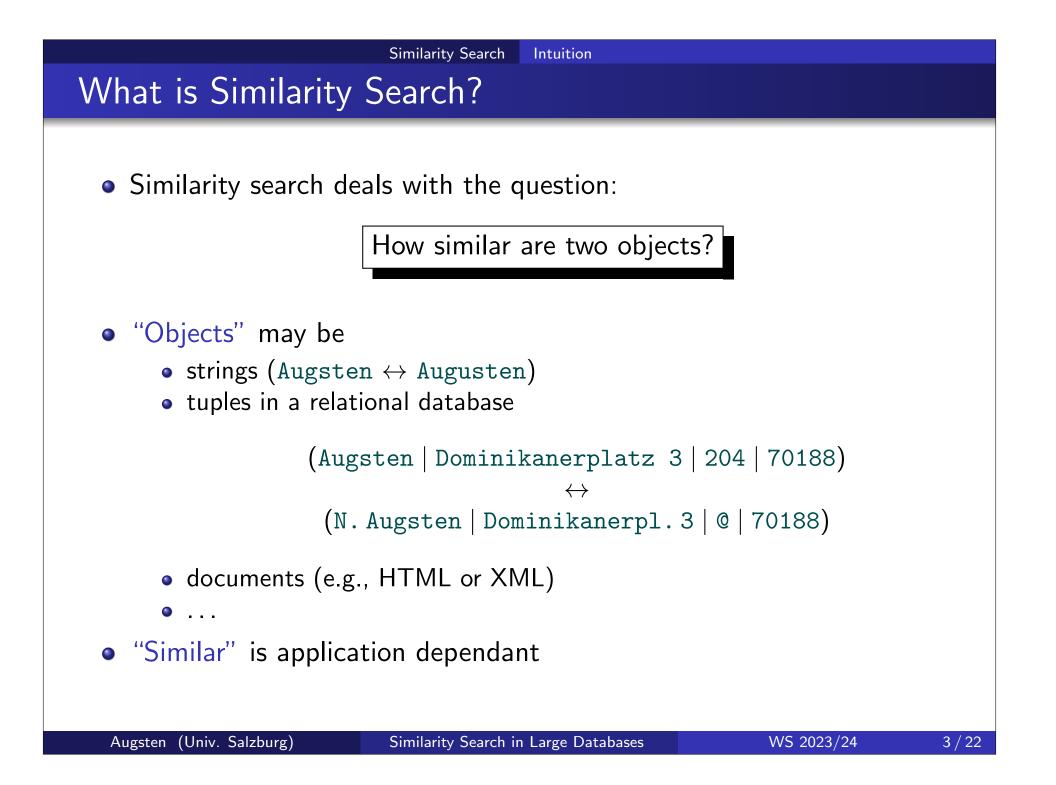




- Intuition
- Applications
- Framework







### Application I: Entity Resolution (ER)

• Problem: (also known as "object identification")

- Two data items represent the same real world object/entity (e.g., the same person),
- but they are represented differently in the database(s).
- How can this happen?
  - different coding conventions (e.g., Gilmstrasse, Hermann-von-Gilm-Str.)
  - spelling mistakes (e.g., Untervigil, Untervigli)
  - outdated values (e.g., Siegesplatz used to be Friedensplatz).
  - incomplete/incorrect values (e.g., missing or wrong apartment number in residential address).

• Focus in this course!

### Application I: Flavors of Entity Resolution

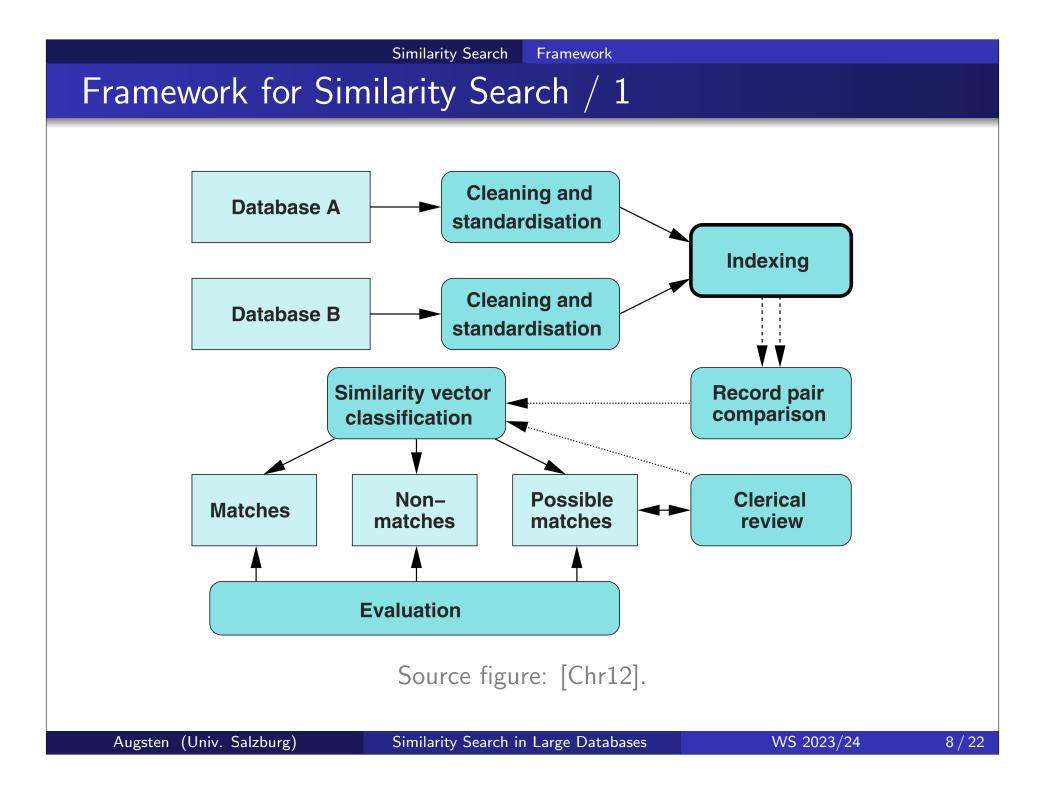
- Duplicate Detection (also: "dirty ER")
  - one table
  - find all tuples in the table that represent the same thing in the real world
  - Example: Two companies merge and must build a single customer database.
- Similarity Join (also: "clean-clean ER")
  - two tables
  - join all tuples with similar values in the join attributes
  - Example: In order to detect tax fraud, data from different databases need to be linked.
- Similarity Lookup
  - one table, one tuple
  - find the tuple in the table that matches the given tuple best
  - Example: Do we already have customer X in the database?

### Application II: Computational Biology

- DNA and protein sequences
  - modelled as text over alphabet (e.g.  $\{A, C, G, T\}$  in DNA)
- Application: Search for a pattern in the text
  - look for given feature in DNA
  - compare two DNAs
  - decode DNA
- Problem: Exact matches fail
  - experimental measures have errors
  - small changes that are not relevant
  - mutations
- Solution: Similarity search
  - Search for *similar* patterns
  - *How similar* are the patterns that you found?

# Application III: Error Correction in Signal Processing

- Application: Transmit text signal over physical channel
- Problem: Transmission may introduce errors
- Goal: Restore original (sent) message
- Solution: Find correct text that is closest to received message.



### Framework for Similarity Search / 2

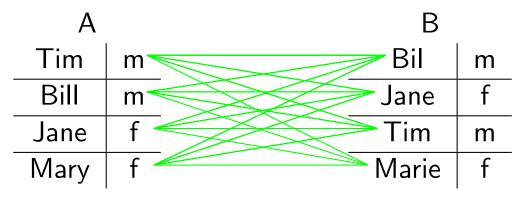
1. Preprocessing: Cleaning and standardization, e.g.

- lowercase all values: Augsten  $\rightarrow$  augsten
- standardize values:  $\{f, w, female, weiblich\} \rightarrow \{f\}$
- standardize encoding: K.Wolf Strasse  $\rightarrow$  Karl-Wolf-Str.
- 2. Indexing for Search Space Reduction
  - blocking
  - sorted-neighborhood
  - filter ing (pruning)
  - nearest neighbor search
- 3. Compute Distances
  - compare record/tuple pairs
- 4. Find Matches: Classification
  - classify record/tuple pairs based on a distance or a vector of distances



### Search Space Reduction: Brute Force

- We consider the example of similarity join.
- Similarity Join: Find all pairs of similar tuples in tables A and B.
  - Search space:  $A \times B$  (all possible pairs of tuples)
  - Complexity: compute |A||B| distances  $\rightarrow$  expensive! (|A| = 30k, |B| = 40k, 1ms per distance  $\Rightarrow$  join will run for 2 weeks)
- Example: 16 distance computations!



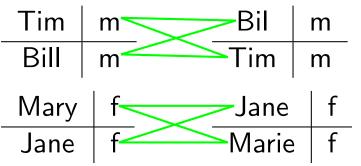
• Goal: Reduce search space!

### Search Space Reduction: Blocking

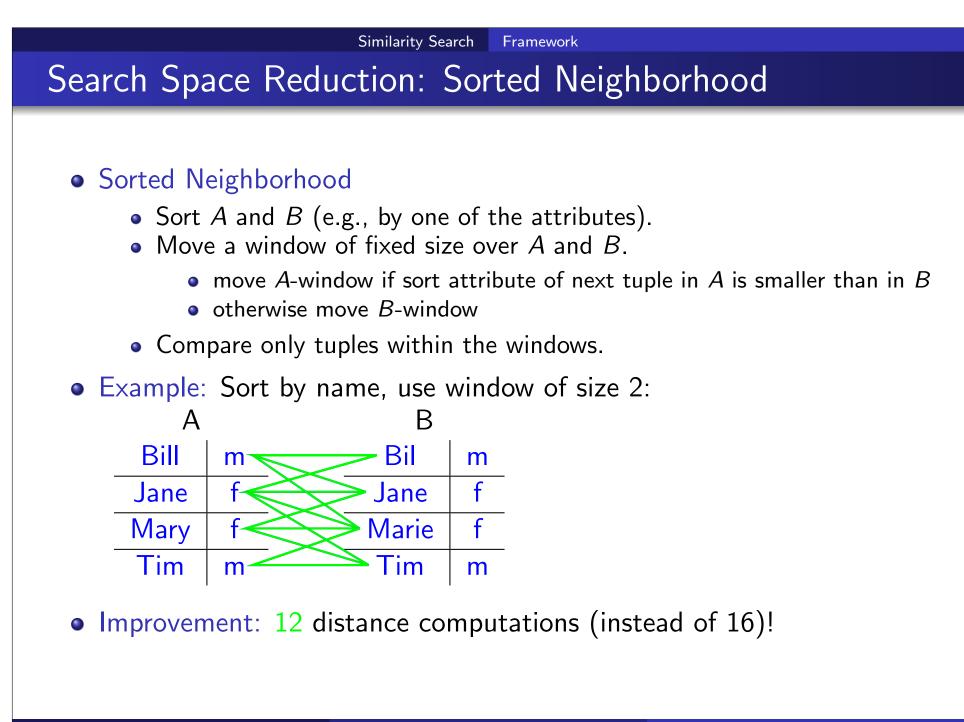
- Blocking
  - Generate blocks for A and B (seperately):
    - 1. compute one or more block keys for each tuple
    - 2. each distinct block key represents one block
    - 3. assign each tuple to all blocks of its block keys
  - Compare only tuples of block pairs with the same block key.

• Example: Attribute blocking: block key is value of a chosen attribute.

Block by "gender" attribute:



• Improvement: 8 distance computations (instead of 16)!

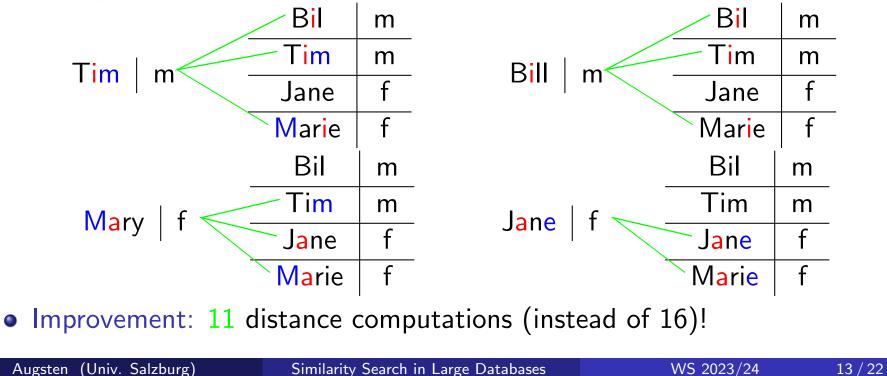


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### Search Space Reduction: Filtering

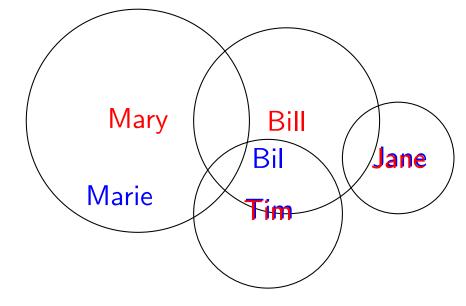
#### • Filtering (Pruning)

- Filter: quick check if tuple pair is "promising" (i.e., distance is expected to be small enough).
- Do not compute distance function if filter check fails.
- Idea: filter is faster than distance function. Overhead for filtering is amortized by avoided distance computations.
- Example: Do not match names that have no character in common:



### Search Space Reduction: Nearest-Neighbor Search

- Represent tuples in some vector space or metric space.
- For each tuple *t* in *A*:
  - search for all tuples in B that are close to tuple t of A
  - distance to t is evaluated only for these tuples of B
- Example: Search for tuples of *A* in tuples of *B*.



• Improvement: 6 distance computations (instead of 16)!

### **Distance** Computation

#### Definition (Distance Function)

Given two sets of objects, A and B, a *distance function* for A and B maps each pair  $(a, b) \in A \times B$  to a positive real number (including zero).

 $\delta: A \times B \to \mathbb{R}^+_0$ 

- We will define distance functions for
  - sets
  - strings
  - trees

### Distance Matrix

#### Definition (Distance Matrix)

Given a distance function  $\delta$  for two sets of objects,  $A = \{a_1, \ldots, a_n\}$  and  $B = \{b_1, \ldots, b_m\}$ . The *distance matrix* D is an  $n \times m$ -matrix with

$$d_{ij} = \delta(a_i, b_j),$$

where  $d_{ij}$  is the element at the *i*-th row and the *j*-th column of *D*.

• Example distance matrix,  $A = \{a_1, a_2, a_3\}$ ,  $B = \{b_1, b_2, b_3\}$ :

	Similarity S	Search	Frame	ework			
Finding Matches							
		$b_1$	$b_2$	$b_3$			
	$a_1$		5		·		
	<i>a</i> 2	2	2 3	1			
	<i>a</i> 3	1	3	0			

- Once we know the distances which objects match?
- Distance matrix and search space reduction:
  - matrix may be only partially filled at the time of computing matches
  - missing distance values are treated as infinite

# Finding Matches: Threshold Matching

Similarity Search

	$b_1$	$b_2$	<i>b</i> <sub>3</sub>
$a_1$	6	5	4
$a_2$	2	2	1
a <sub>3</sub>	1	3	0

Framework

#### • Threshold Approach:

- fix threshold  $\tau$
- $\bullet\,$  for a given object, all objects with a distance range of  $\tau\,$  are matched
- Algorithm: produces *n*:*m* matching

foreach  $d_{ij} \in D$  do if  $d_{ij} \leq \tau$  then match  $(a_i, b_j)$ 

• Example with  $\tau = 2$ : {( $a_2, b_1$ ), ( $a_2, b_2$ ), ( $a_2, b_3$ ), ( $a_3, b_1$ ), ( $a_3, b_3$ )}

# Finding Matches: k-Nearest Neighbor Matching

Similarity Search

	$b_1$	$b_2$	<i>b</i> <sub>3</sub>
$a_1$	6	5	4
<i>a</i> 2	2	2	1
a <sub>3</sub>	1	3	0

Framework

- k-Nearest-Neighbor (kNN) Matching:
  - fix number of neighbors k
  - for a given object, form a match with its k nearest neighbors
- Algorithm: produces 1:k matching

foreach row *i* of distance matrix *D* do

find column IDs  $c_1, c_2, \ldots, c_k$  of k smallest values in row i of D form k matches  $(a_i, b_{c_1}), (a_i, b_{c_2}), \ldots, (a_i, b_{c_k})$ 

#### • Properties:

- not symmetric: transposed matrix  $D^T$  may give a different result
- ties affect the matching (only for k-th neighbor)
- Example k = 2: {( $a_1, b_3$ ), ( $a_1, b_2$ ), ( $a_2, b_3$ ), ( $a_2, b_1$ ), ( $a_3, b_3$ ), ( $a_3, b_1$ )}

### Finding Matches: Global Greedy

 Global Greedy Approach • form object pair with smallest distance first matched objects are removed • Algorithm: produces 1:1 matching  $M \leftarrow \emptyset$  $A \leftarrow \{a_1, a_2, \dots, a_n\}; B \leftarrow \{b_1, b_2, \dots, b_m\}$ create sorted list *L* with all  $d_{ii} \in D$ while  $A \neq \emptyset$  and  $B \neq \emptyset$  do  $d_{ii} \leftarrow$  deque smallest element from L if  $a_i \in A$  and  $b_i \in B$  then  $M \leftarrow M \cup (a_i, b_i)$ remove  $a_i$  from A and  $b_i$  from B return M • Properties: must deal with ties when sorting list L, e.g., sort ties randomly, sort ties by i and j

• Example (sort ties by i, j):  $\{(a_3, b_3), (a_2, b_1), (a_1, b_2)\}$ 

	$b_1$	$b_2$	<i>b</i> <sub>3</sub>
$a_1$	6	5	4
$a_2$	2	2	1
<i>A</i> 2	1	3	0

#### **Overview:** Matching Techniques

#### • Threshold Matching:

- all objects with distance within au match
- *n*:*m*-matching
- symmetric, not affected by ties
- *k*-Nearest Neighbor Matching:
  - each object is matched to its k closest objects
  - 1:*k*-matching
  - not symmetric, affected by ties
- Global Greedy Approach:
  - pair with smallest distance is matched first and removed
  - 1:1-matching
  - symmetric, affected by ties

# Conclusion

#### • Framework for similarity queries:

- 1. Preprocessing: Cleaning and standardization
- 2. Indexing for Search Space Reduction
  - blocking
  - sorted-neighborhood
  - filtering (pruning)
  - nearest neighbor search
- 3. Compute Distances
- 4. Find Matches: Classification
  - threshold-based
  - k-nearest-neighbor
  - global greedy



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#### Peter Christen.

A survey of indexing techniques for scalable record linkage and deduplication.

IEEE Trans. Knowl. Data Eng., 24(9):1537–1555, 2012.