Similarity Search The q-Gram Distance

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Filters for the Edit Distance

Outline

- Filters for the Edit Distance
 - Motivation
 - Lower Bound Filters
 - Length Filter
 - q-Grams: Count Filter
 - q-Grams: Position Filtering
 - Experiments
- Conclusion

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- 2 The q-Gram Distance
- 3 Conclusion

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Filters for the Edit Distance Motivation

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Filters for the Edit Distance Motivation

Application Scenario

- Scenario:
 - A company offers a number of services on the Web.
 - You can subscribe for each service independently.
 - Each service has its own database (no unique key across databases).
- Example: customer tables of two different services:

Α				В			
ID	ID name			ID	name		
1023	Frodo Baggins			948483	John R. R. Tolkien		
21	J. R. R. Tolkien			153494	C. S. Lewis		
239	C.S. Lewis			494392	Fordo Baggins		
863	Bilbo Baggins			799294	Biblo Baggins		

Task: Created unified customer view!

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Filters for the Edit Distance Motivation

Effectiveness and Efficiency of the Approximate Join

• Effectiveness: Join result for k = 3:

name	ID	name				
Frodo Baggins	494392	Fordo Baggins				
J. R. R. Tolkien	948483	John R. R. Tolkien				
C.S. Lewis	153494	C. S. Lewis				
Bilbo Baggins	799294	Biblo Baggins				
	Frodo Baggins J. R. R. Tolkien C.S. Lewis	Frodo Baggins 494392 J. R. R. Tolkien 948483 C.S. Lewis 153494				

- \Rightarrow very good (100% correct)
- Efficiency: How does the DB evaluate the query?
 - (1) compute $A \times B$
 - (2) evaluate UDF on each tuple $t \in A \times B$
- Prohibitive runtime!

Filters for the Edit Distance Motivation

The Join Approach

• Solution: Join customer tables on name attribute (Q1):

SELECT * FROM A,B WHERE A.name = B.name

- Exact Join: Does not work!
- Similarity Join: Allow k errors...
 - (1) Register UDF (User Defined Function) for the edit distance:

ed(x, y)

returns the union cost edit distance between the strings x and y.

(2) Rewrite query Q1 as similarity join (Q2):

SELECT * FROM A,B WHERE ed(A.name, B.name) <= k

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Filters for the Edit Distance Motivation Using a Filter for Search Space Reduction

- Search space: $A \times B$ ($\Rightarrow |A| \cdot |B|$ edit distance computations)
- Filtering (Pruning): Remove tuples that can not match, without actually computing the distance.

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Filters for the Edit Distance Lower Bound Filters

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Filters for the Edit Distance Lower Bound Filters

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Lower Bound Filters

• Lower bound (lb) for distance dist(x, y):

$$dist(x, y) \ge lb_{dist}(x, y)$$

• Query Q3 with Lower Bound Filter:

- 1b(A.name, B.name) is a cheap function
- database will optimize query: compute ed(A.name, B.name) only if $lb(A.name, B.name) \leq k$
- No false negatives!

Filters for the Edit Distance Lower Bound Filters

Filter Properties

• Error Types:

Correct Result

		positive	negative
Filter	positive	true positive	false positive
Test	negative	false negative	true negative

- Example: "Are x and y within edit distance k?"
 - Correct result: compute edit distance and test ed(x, y) < k
 - Filter test: give answer without computing edit distance
 - False negatives: x and y are pruned although ed(x, y) < k.
 - False positives: x and y are not pruned although $ed(x, y) \leq k$.
- Good filters have
 - no false negatives (i.e., miss no correct results)
 - few false positive (i.e., avoid unnecessary distance computations)

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Filters for the Edit Distance Length Filter

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Augsten (Univ. Salzburg) Similarity Search WS 2023/24 11 / 44 Augsten (Univ. Salzburg) Similarity Search Filters for the Edit Distance Length Filter

Length Filtering

Theorem (Length Filtering [GIJ+01])

If two strings x and y are within edit distance k, their lengths cannot differ by more than k:

$$\operatorname{ed}(x,y) \ge \operatorname{abs}(|x| - |y|)$$

- Proof: At least abs(|x|-|y|) inserts are needed to bring x and y to the same length.
- Query Q4 with Length Filtering:

```
SELECT * FROM A,B
WHERE ABS(LENGTH(A.name)-LENGTH(B.name)) <= k AND
      ed(A.name, B.name) <= k
```

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Similarity Search Filters for the Edit Distance q-Grams: Count Filter WS 2023/24

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Filters for the Edit Distance Length Filter

Example: Length Filtering

• Execute query without/with length filter (k = 3):

Α			В		
ID name			ID	name	
1023	Frodo Baggins ₁₃	_	948483	John R. R. Tolkien ₁₈	
21	J. R. R. Tolkien ₁₆		153494	C. S. Lewis ₁₁	
239	C.S. Lewis ₁₀		494392	Fordo Baggins ₁₃	
863	Bilbo Baggins ₁₃		799294	Biblo Baggins ₁₃	

- Without length filter: 16 edit distance computations
- With length filter (k = 3): 12 edit distance computations
 - \bullet J. R. R. Tolkien \leftrightarrow C. S. Lewis is pruned
 - all pairs (..., John R. R. Tolkien) except (J. R. R. Tolkien, John R. R. Tolkien) are pruned

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Filters for the Edit Distance q-Grams: Count Filter

What is a q-Gram?

- Intuition:
 - slide window of length q over string $x \in \Sigma^*$
 - characters covered by window form a q-gram
 - where window extends string: fill with dummy character # $\notin \Sigma$
- Example: x = Frodo, q = 3extended: ##Frodo## q-grams: ##F #Fr Fro
 - rod odo d o# 0##
- q-Gram Profile G_x : bag of all q-grams of x
- Profile size: $|G_x| = |x| + q 1$

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Single Edit Operations and Changing *q*-Grams

- Intuition: Strings within small edit distance share many q-grams.
- How many q-grams (q = 3) change/remain?

X		$ G_x $	y	$ G_y $	$ G_x \cap G_y $
pete	er	7	meter	7	4
pete	er	7	peters	8	5
pete	er	7	peer	6	4

 \bullet ed $(x, y) = 1 \Rightarrow |G_x \cap G_y| = \max(|G_x|, |G_y|) - a$

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Filters for the Edit Distance q-Grams: Count Filter

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Count Filtering

Theorem (Count Filtering [GIJ+01])

Consider two strings x and y with the q-gram profiles G_x and G_y , respectively. If x and y are within edit distance k, then the cardinality of the a-gram profile intersection is at least

$$|G_x \cap G_y| \ge \max(|G_x|, |G_y|) - kq$$

- Proof (by induction):
 - true for k = 1: $|G_x \cap G_y| \ge \max(|G_x|, |G_y|) q$
 - $k \rightarrow k + 1$: each additional edit operation changes at most q *q*-grams.

Multiple Edit Operations and Changing q-Grams

- \bullet ed $(x, y) = 1 \Rightarrow |G_x \cap G_y| = \max(|G_x|, |G_y|) q$
- What if ed(x, y) = k > 1?

X	$ G_x $	y	$ G_y $	$ G_x \cap G_y $
peter	7	meters	8	2
peter	7	petal	7	3

• Multiple edit operations may affect the same q-gram:

$$peter \rightarrow G_x = \{ \#p, \#pe, pet, ete, ter, er\#, r\#\# \}$$

$$petal \rightarrow G_y = \{ \#p, \#pe, pet, eta, tal, al\#, l\#\# \}$$

• Each edit operation affects at most q q-grams.

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Filters for the Edit Distance q-Grams: Count Filter

Implementation of q-Grams

- Given: tables A and B with schema (id, name)
 - *id* is the key attribute
 - name is string-valued
- Compute auxiliary tables QA and QB with schema (id, qgram):
 - each tuple stores one *q*-gram
 - string x of attribute name is represented by its |x| + q 1 q-grams
 - QA.id is the key value (A.id) of a tuple with A.name = x
 - QA.qgram is one of the q-grams of x
- Example:

	Α	QA		
id	name	id	qgram	
1023	Frodo Baggins	1023	##F	
21	J. R. R. Tolkien	1023	#Fr	
239	C.S. Lewis			
863	Bilbo Baggins	21	##J	
		21	#J.	

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Filters for the Edit Distance q-Grams: Count Filter

Count Filtering Query

Query Q5 with Count Filtering:

```
SELECT
        A.id, B.id, A.name, B.name
FROM
         A, QA, B, QB
WHF.R.F.
         A.id = QA.id AND
         B.id = QB.id AND
         QA.qgram = QB.qgram AND
         ABS(LENGTH(A.name)-LENGTH(B.name)) <= k
GROUP BY A.id, B.id, A.name, B.name
        COUNT(*) >= LENGTH(A.name)-1-(k-1)*q AND
HAVING
         COUNT(*) >= LENGTH(B.name)-1-(k-1)*q AND
         ed(A.name,B.name) <= k
```

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Fixing Count Filtering Query

Filters for the Edit Distance q-Grams: Count Filter

- Fix query to avoid false negatives [GIJ+03]:
 - Join pairs (x, y) with $kq \ge \max(|G_x|, |G_y|)$ using only length filter.
 - Union results with results of previous query Q5.
- Query Q6 without false negatives (extends previous query Q5):

UNION SELECT A.id, B.id, A.name, B.name FROM A, B WHERE LENGTH(A.name)+ $q-1 \le k*q$ AND $LENGTH(B.name)+q-1 \le k*q AND$ ABS(LENGTH(A.name) - LENGTH(B.name)) <= k AND ed(A.name,B.name) <= k

• Note: We omit this part in subsequent versions of the query since it remains unchanged.

Filters for the Edit Distance q-Grams: Count Filter

Problem with Count Filtering Query

- Previous guery Q5 works fine for $kq < \max(|G_x|, |G_y|)$.
- However: If $kq \ge \max(|G_x|, |G_v|)$, no q-grams may match even if $ed(x, y) \le k$.
- Example (q = 3, k = 2):

WHERE-clause prunes x and y, although $ed(x, y) \le k$

- False negatives:
 - short strings with respect to edit distance (e.g., |x| = 3, k = 3)
 - even if within given edit distance, matches tend to be meaningless (e.g., abc and xyz are within edit distance k = 3)

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Filters for the Edit Distance q-Grams: Position Filtering

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Filters for the Edit Distance q-Grams: Position Filtering

Positional q-Grams

- Enrich *q*-grams with position information:
 - extended string: prefix and suffix string x with q-1 characters #
 - slide window of length q over extended string x'
 - characters covered by window after shifting it *i* times form the *q*-gram at position i + 1
- Example: x = Frodo

```
extended string:
                        ##Frodo##
positional q-grams: (1, \# F)
                      (2, \# Fr)
                        (3.Fro)
                          (4,rod)
                           (5, odo)
                             (6,d o \#)
                              (7.0 # #)
```

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Filters for the Edit Distance q-Grams: Position Filtering

Corresponding *q*-Grams

- Corresponding *q*-gram:
 - Given: positional q-grams (i, g) of x
 - transform x to y applying edit operations
 - (i,g) "becomes" (i,g) in y
 - We define: (i,g) corresponds to (i,g)
- Example:
 - x' = #abaZabaabaaba##, y' = #abaabaabaabaaba##
 - edit distance is 1 (delete Z from x)
 - (7, aba) in x corresponds to (6, aba) in y
 - ... but not to (9, aba)

Filters for the Edit Distance q-Grams: Position Filtering

Computing Positional q-Grams in SQL

- Given: table N
 - N has a single attribute i
 - N is filled with numbers from 1 to max (max is the maximum string length plus q-1)
- Positional q-grams for table A in SQL (Q7):

```
CREATE TABLE QA AS
       SELECT A.id, N.i AS pos,
           SUBSTRING (CONCAT (
               SUBSTRING('\#..\#', 1, q - 1),
               LOWER(A.name),
               SUBSTRING('#..#', 1, q - 1)),
           N.i, q) AS ggram
       FROM A, N
       WHERE N.i <= LENGTH(A.name) + q - 1
```

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Filters for the Edit Distance q-Grams: Position Filtering

Position Filtering

Theorem (Position Filtering [GIJ+01])

If two strings x and y are within edit distance k, then a positional q-gram in one cannot correspond to a positional q-gram in the other that differs from it by more then k positions.

- Proof:
 - each increment (decrement) of a position requires an insert (delete);
 - a shift by k positions requires k inserts/deletes.

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Filters for the Edit Distance q-Grams: Position Filtering

Position Filtering

• Query Q8 with Count and Position Filtering:

A.id, B.id, A.name, B.name

FROM A, QA, B, QB

WHERE A.id = QA.id AND

B.id = QB.id AND

QA.qgram = QB.qgram AND

ABS(LENGTH(A.name)-LENGTH(B.name)) <= k AND

ABS(QA.pos-QB.pos)<=k

GROUP BY A.id, B.id, A.name, B.name

COUNT(*) >= LENGTH(A.name)-1-(k-1)*q ANDHAVING

COUNT(*) >= LENGTH(B.name)-1-(k-1)*q AND

ed(A.name, B.name) <= k

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Similarity Search Filters for the Edit Distance Experiments WS 2023/24

Outline

Filters for the Edit Distance

Lower Bound Filters

• q-Grams: Count Filter

• q-Grams: Position Filtering

Motivation

Length Filter

Experiments

Experimental Data

- All experimental results taken from [GIJ⁺01]
- Three string data sets:
 - set1: 40K tuples, average length: 14 chars
 - set2: 30K tuples, average length: 38 chars
 - set3: 30K tuples, average length: 33 chars

Conclusion WS 2023/24 Augsten (Univ. Salzburg) Similarity Search Filters for the Edit Distance Experiments String Length Distributions **№** 10000 8000 6000 4000 11 16 21 17 25 33 41 String Length Set 1 Set 2 - Proceedings of the Contraction 15 22 29 36 43 String Length Set 3

Filters for the Edit Distance Experiments

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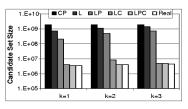
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Filters for the Edit Distance Experiments

Candidate Set Size

- Question: How many edit distances do we have to compute?
- Show candidate set size for different filters (small is good).
- q = 2
- Caption:
 - CP: cross product
 - L: length filtering, P: position filtering, C: count filtering
 - Real: number of real matches



Set 1

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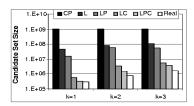
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Filters for the Edit Distance Experiments

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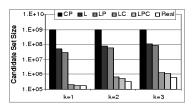


Set 3

Filters for the Edit Distance Experiments

Candidate Set Size

- Question: How many edit distances do we have to compute?
- Show candidate set size for different filters (small is good).
- q = 2
- Caption:
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 - L: length filtering, P: position filtering, C: count filtering
 - Real: number of real matches



Set 2

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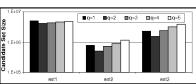
Filters for the Edit Distance Experiments

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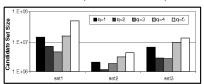
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Various q-Gram Lengths

- Question: How does the choice of *q* influence the filter effectiveness?
- Show candidate set size for different q values (small is good).



Edit Distance Threshold k = 2



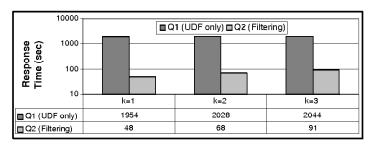
Edit Distance Threshold k = 3

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Filters for the Edit Distance Experiments

Response Time

- Approximate self-join on small sample of 1000 tuples (set 1) (full dataset > 3 days without filters!)
- Measure response time (small is good).
- Caption:
 - k: edit distance threshold
 - Q1: edit distance without filters
 - Q2: edit distance with filters



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The q-Gram Distance

The q-Gram Distance

Definition (q-Gram Distance [Ukk92])

Let G_x and G_y be the q-gram profiles of the strings x and y, respectively. The *q-gram distance* between two strings is the number of *q*-grams in G_x and G_v that have no match in the other profile,

$$\mathsf{dist}_q(x,y) = |G_x \uplus G_y| - 2|G_x \cap G_y|.$$

• Example: q = 2, x = abab, y = abcab

$$G_{x} = \{ \text{#a}, \text{ab}, \text{ba}, \text{ab}, \text{b#} \}$$

$$G_{v} = \{ \text{#a, ab, bc, ca, ab, b#} \}$$

$$G_x \uplus G_y = \{\text{\#a,ab,ba,ab,b\#,\#a,ab,bc,ca,ab,b\#}\}$$

$$G_x \cap G_y = \{\text{#a, ab, ab, b#}\}$$

$$dist_{a}(x, y) = |G_{x} \uplus G_{y}| - 2|G_{x} \cap G_{y}| = 11 - 2 \cdot 4 = 3$$

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The g-Gram Distance

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The g-Gram Distance

Pseudo Metric q-Gram Distance

- The q-gram distance is a pseudo metric: For all $x, y, z \in \Sigma^*$
 - $\operatorname{dist}_q(x,y) + \operatorname{dist}_q(y,z) \ge \operatorname{dist}_q(x,z)$ (triangle inequality)
 - $\operatorname{dist}_{a}(x, y) = \operatorname{dist}_{a}(y, x)$ (symmetric)
 - $\operatorname{dist}_{a}(x, y) = 0 \Leftarrow x = y$
- Note: Identity condition relaxed: dist_a $(x, y) = 0 \Rightarrow x = y$ i.e., the q-gram distance between two different strings can be 0
- Example:

$$\begin{aligned} &\mathsf{dist}_q(\mathsf{axybxycxyd}, \mathsf{axycxybxyd}) = 0 \\ &G_x = G_y = \{ \texttt{\##a}, \texttt{\#ax}, \mathsf{axy}, \mathsf{xyb}, \mathsf{ybx}, \mathsf{bxy}, \mathsf{xyc}, \mathsf{ycx}, \mathsf{cxy}, \mathsf{xyd}, \mathsf{yd\#}, \mathsf{d\#\#} \} \end{aligned}$$

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The g-Gram Distance

Distance Normalization (1/3)

• What is a good threshold?

```
ed(International Business Machines Corporation,
    International Bussiness Machine Corporation) = 2
ed(IBM, BMW) = 2
ed(Int. Business Machines Corp.,
    International Business Machines Corporation) = 17
```

- Problem: Absolute numbers not always meaningful...
- Solution: Compute error relative to string length!

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The q-Gram Distance

Distance Normalization (3/3)

Normalized edit distance:

```
\label{eq:corporation} \begin{array}{ll} \text{norm-ed(International Business Machines Corporation}, \\ & \text{International Bussiness Machine Corporation}) = 0.047 \\ \text{norm-ed(IBM, BMW)} = 0.66 \\ \text{norm-ed(Int. Business Machines Corp.}, \\ & \text{International Business Machines Corporation}) = 0.4 \\ \end{array}
```

• Normalized q-gram distance (q = 3):

```
\begin{aligned} & \text{norm-dist}_q(\text{International Business Machines Corporation}, \\ & & \text{International Bussiness Machine Corporation}) = 0.089 \\ & \text{norm-dist}_q(\text{IBM}, \text{BMW}) = 1.0 \\ & \text{norm-dist}_q(\text{Int. Business Machines Corp.}, \\ & & \text{International Business Machines Corporation}) = 0.36 \end{aligned}
```

The g-Gram Distance

Distance Normalization (2/3)

- Normalize distance such that $\delta(x, y) \in [0..1]$
- Edit Distance:
 - non-normalized: $0 \le \operatorname{ed}(x, y) \le \max(|x|, |y|)$
 - normalized edit distance: $0 \le \text{norm-ed}(x, y) \le 1$

$$\mathsf{norm\text{-}ed}(x,y) = \frac{\mathsf{ed}(x,y)}{\mathsf{max}(|x|,|y|)}$$

- q-Gram Distance:
 - non-normalized: $0 \le \operatorname{dist}_q(x, y) \le |G_x \uplus G_y| |G_x \cap G_y|$
 - normalized q-gram distance: $0 \le \text{norm-dist}_q(x, y) \le 1$

$$\mathsf{norm\text{-}dist}_q(x,y) = \frac{\mathsf{dist}_q(x,y)}{|\mathit{G}_x \uplus \mathit{G}_y| - |\mathit{G}_x \cap \mathit{G}_y|} = 1 - \frac{|\mathit{G}_x \cap \mathit{G}_y|}{|\mathit{G}_x \uplus \mathit{G}_y| - |\mathit{G}_x \cap \mathit{G}_y|}$$

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Edit Distance vs. q-Gram Distance

Edit distance can not handle block-moves well:

$$x = \text{Nikolaus Augsten}$$
 $y = \text{Augsten Nikolaus}$
 $norm-ed(x, y) = 1.0$
 $norm-dist_a(x, y) = 0.39$ $(q = 3)$

The g-Gram Distance

• q-Gram distance may be too strict:

```
x = +39-06-46-74-22 y = (39\ 06\ 467422)

norm-ed(x,y) = 0.4

norm-dist_q(x,y) = 1.0 (q = 3)
```

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¹Jaccard normalization. Dividing by $|G_x \uplus G_y|$ (Dice normalization) also normalizes to [0..1], but the metric properties (triangle inequality) get lost [ABG10].



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Approximate string-matching with q-grams and maximal matches.

Approximate join with edit distance inefficient.
Edit distance filters speed up join:

Length filter: based on the string length
Count filter: based on q-Grams
Position filter: based on positional q-Grams

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